

# Climate and the NZ Electricity Spot Market

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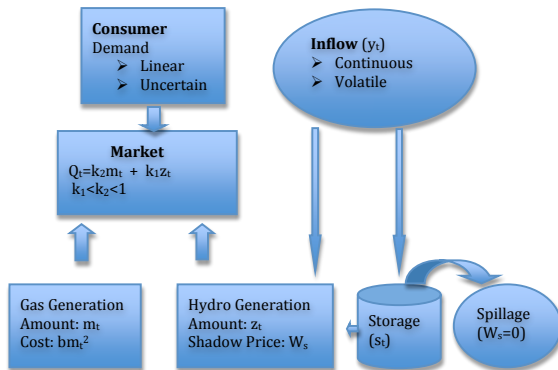
Presentation at the Motu Climate Economics Workshop  
Draws on work of Lewis Evans, Graeme Guthrie, Andrea Lu and John Nash

# Outline

- 1 The Electricity Market
- 2 Decision making with uncertain demand and inflows
- 3 The Base case
- 4 Outcomes of competition and monopoly
- 5 Effects of changes in climate (inflows/carbon tax)
- 6 Possibilities

# The Spot Market

## The Market



# New Zealand Electricity Market Calibration 2007

- Quantity:  $q$  is TWh
- Demand curve:  $P(q) = 185 - 3.47q$  [plus price shocks for a given quantity]  
*elasticity of demand* = 0.4 (Borenstein and Bushnell, 1998)
- $k_1 = 0.956$  (Otahuhu-Benmore)  
 $k_2 = 0.984$  (Otahuhu-Hayward)
- Generation Capacity  $\bar{z} = 47$  and  $\bar{m} = 35$  TWh/y
- Lake Capacity  $\bar{s} = 4.44$  TWh
- The risk-free interest rate  $r = 0.04$
- Cost of gas:  $C(m) = 0.7112m^2$ 
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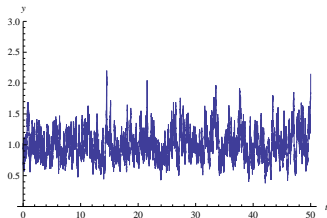
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# 50 Years of Daily Inflows

- stationary diffusion process: with mean = 1
- increment in inflow = mean reversion\*(1-inflow) + shock (affected by variance and inflow level)
- $dy_t = 6.9448(1 - y_t)dt + 0.9056\sqrt{y_t}d\epsilon_t$



# Social Planner Objectives I

- Given  $m_t$  and  $z_t$ , the flow of net social benefit at date  $t$  is

$NSB(z_t, m_t, y_t) = \text{Area under demand curve less cost of gas generation}$

- No other use for water and reservoir fixed cost, so no water cost in flow of net social benefit
- Social planner's ultimate interest is in maximizing the *expected present value* of net social benefit

$$W(s, y) = E_0 \left[ \int_0^{\infty} e^{-rt} NSB(z_t, m_t) dt \right]$$

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## Intertemporal equilibrium

- <1-> Given generation policy  $(m, z)$ , total welfare  $W$  must satisfy

$$\underbrace{rW}_{\text{"required return"}} = \underbrace{NSB(m, z, y)}_{\text{Net Social Benefit}} + \underbrace{(y - z) \frac{\partial W}{\partial s} + \nu \frac{\partial W}{\partial y} + \frac{1}{2} \phi^2 \frac{\partial^2 W}{\partial y^2}}_{\text{expected social "capital gain"}}$$

expected "total return"

- The value of marginal unit of stored water,  $\frac{\partial W}{\partial s}$ , appears as an element of expected social capital gain.
- Planner chooses generation  $(m, z)$  to maximize RHS of required return : that is, maximise the social planner's "short-run" objective function

$$NSB(m, z, y) - \text{cost of water} = \text{area under demand curve} - c(m) - z \underbrace{\frac{\partial W}{\partial s}}_{\text{generation cost:}}$$

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# Summary:

the social planner decisions = competitive market

- generation decisions are
  - static but linked to future by the shadow price of stored water
  - based upon inflows and stored fuel
  - forward looking (expectations)
  - affected by volatility in inflows and demand
- outcomes and economic welfare are affected by
  - the structure of demand and supply
    - e.g shape of demand
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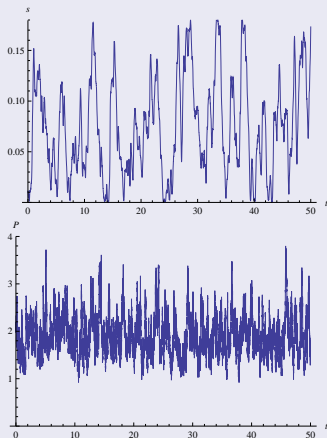
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# The Base Case Under Competition

Monopoly higher price, lower volatility

## Storage and Price



# The Base Case Under Competition

associations

## Correlations

- shadow price with
  - storage: -0.83
  - inflows: -0.72
  - gas generation: 0.99
- Hydro generation with
  - storage: 0.78
  - inflows: 0.71
  - gas:-0.91
- inflow with
  - price: -0.18

## Explore by

- 1 Varying mean (average) inflows
- 2 Varying forecastability (volatility of inflows)
- 3 Carbon tax

# Changes in Mean Inflows

Decrease average inflow by 30%

- NIWA argues that inflow will actually increase
- Decrease in average inflow means increased amount of low-cost fuel over any reasonable period

Relative to Base	Competition	Monopoly
Hydro G	70%	71%
Gas G	1.26%	2.83%
Social W	91%	93%
Profit	1.04	96%
Social Value Extra Capacity	31%	17%
Market Value Capacity	44%	70%

Volatility spread between competition and monopoly remains

# Reduced Inflow Predictability

Decrease mean reversion parameter by 30%

Increases overall variability as well

Relative to Base	Competition	Monopoly
Hydro G	100%	98%
Gas G	100%	112%
Social W	100%	100%
Profit	99%	100%
Social Value Extra Capacity	223%	158%
Market Value Extra Capacity	174%	156%

Volatility spread between competition and monopoly remains

Big increase in the value of extra reservoir



# Carbon Tax

\$25/tCO<sub>2</sub> = 25% increase in mc of gas

Price increase less than half the increase in marginal cost

Relative to Base Case	Competition	Monopoly
Hydro G	100%	100%
Gas G	90%	93%
Social W	98%	99%
Profit	109%	100%
Social Value capacity	115%	114%
Market Value capacity	113%	113%
Price	112%	1.01

## Developments

- more on random demand and correlation with inflows
- other oligopoly market structures
  - oligopoly with mixed portfolios
  - oligopoly with specialised portfolios
  - other forms of competition
- Cap and Trade would be a particular challenge

## References

- 1 Evans, Lewis, Graeme Guthrie and Andrea Lu, *A Continuous-Time Electricity Market Model and its Application to Evaluation of Effects of Climatic Change*, available at SSRN, [http://papers.ssrn.com/sol3/papers.cfm?abstract\\_id=1968028](http://papers.ssrn.com/sol3/papers.cfm?abstract_id=1968028), Dec 2011 20p.